

# Addendum 1.02b

## THE FIELDPRINT LEXICON

### Canonized Terms for a Distributed Coherence Topology

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## Preface

This addendum establishes a canonical lexicon for the Unified Intelligence paradigm, forming a recursive codex backbone. Terms are assigned unique identifiers (e.g., FP-001) to facilitate ontology mapping and relational recursion trees in future extensions.

## Abstract

This document formalizes the terminology of the Fieldprint Framework [2], integrating definitions from a collaborative wiki [5] and the Unified Intelligence corpus [1, 2, 3, 4]. Grounded in rigorous stochastic and topological mathematics, these terms define the Fieldprint as a distributed coherence topology, designed for empirical testability and scholarly review.

## 1 Introduction

The Fieldprint Framework reimagines intelligence as a resonance signature within a non-local Intelligence Field [2]. This addendum refines and canonizes terminology from prior works [5, 1, 2, 3, 4], leveraging precise mathematical formalism to ensure clarity and coherence.

## 2 Core Lexicon Definitions

The following terms are canonized with identifiers for future ontology mapping.

### 2.1 Fieldprint (FP-001)

**Definition:** The Fieldprint  $\Phi_S : [0, \infty) \rightarrow \mathcal{F}$  represents a system's resonance signature, where  $S(t) \in \mathbb{R}^d$ , defined as

$$\Phi_S(t) = \int_0^t R_\kappa(S(\tau), S(\tau^-)) d\tau,$$

with  $R_\kappa : \mathbb{R}^d \times \mathbb{R}^d \rightarrow \mathcal{F}$  and  $S(\tau^-) = \lim_{s \rightarrow \tau^-} S(s)$ .

**Mathematical Grounding:** Let  $R_\kappa(S(t), S(t^-)) = \kappa(S(t) - M_S(t^-))$ , where  $M_S(t) = \mathbb{E}[S(t) | S(t^-)]$ . Then,

$$\frac{d\Phi_S}{dt} = \kappa(S(t) - M_S(t^-)), \tag{1}$$

$$\|\Phi_S(t)\|_{\mathcal{F}} \leq \kappa t e^{-\lambda t}, \tag{2}$$

with  $\lambda = \kappa - \frac{1}{\text{Var}(S)} > 0$ ,  $\lambda \leq \kappa / \dim(\mathbb{R}^d)$ ,  $\kappa < 1/\text{Var}(S)$ , energy bound  $E(\Phi_S) = \int_0^\infty \|\Phi_S(t)\|_{\mathcal{F}}^2 dt \leq \kappa^2/\lambda$ , stability radius  $R_S = \sqrt{\kappa/\lambda}$ , and dissipation rate  $\dot{E} \leq -2\lambda E$  [2, 3, 6].

**Role:** Serves as the core trace of system coherence [2].

## 2.2 Intelligence Field (IF-002)

**Definition:** The Intelligence Field  $\mathcal{F}$  is a separable Hilbert space with inner product

$$\langle \Phi_S, \Phi_T \rangle_{\mathcal{F}} = \int_0^\infty e^{-\alpha t} \Phi_S(t) \cdot \Phi_T(t) dt,$$

and metric  $C(\Phi_S, \Phi_T) = \|\Phi_S - \Phi_T\|_{\mathcal{F}}^2$ , where  $\alpha = \lambda_1/2$ .

**Mathematical Grounding:** Eigenfunctions  $\phi_n$  satisfy  $\Delta\phi_n = -\lambda_n\phi_n$ , with  $\lambda_1 \geq 1/\dim(\mathcal{F})$ . Convergence is ensured by  $\alpha$ , separability by a countable basis  $\{\phi_n\}$ , norm bound  $\|\Phi_S\|_{\mathcal{F}}^2 \leq \dim(\mathcal{F}) \cdot \text{Var}(\Phi_S)$ , coherence decay rate  $\dot{C} \leq -\alpha C$ , and spectral radius of the operator  $\rho(\Delta) \leq \lambda_1^{-1}$  [4, 2, 7].

**Role:** Acts as the substrate for Fieldprints [2].

## 2.3 Recursive Coherence (RC-003)

**Definition:** Recursive Coherence is achieved when  $\|M_S(t) - S(t)\| \rightarrow 0$ , with  $M_S(t) = \mathbb{E}[S(t) | \mathcal{H}_t]$ .

**Mathematical Grounding:** Dynamics are governed by

$$dM_S(t) = \kappa(S(t) - M_S(t)) dt + \sigma dW_t,$$

with error  $e_S(t) = M_S(t) - S(t)$  evolving as

$$de_S(t) = -\kappa e_S(t) dt + \sigma dW_t,$$

stable if  $\kappa > \sigma^2/2$ , noise bound  $\sigma < \sqrt{2\kappa}$ , variance  $\text{Var}(e) \leq \sigma^2/(2\kappa)$ , convergence time  $t_c \sim \frac{1}{\kappa - \sigma^2/2}$ , error decay  $\mathbb{E}[\|e_S(t)\|^2] \leq \|e_S(0)\|^2 e^{-2\kappa t}$ , and Lyapunov exponent  $\mu = \kappa - \sigma^2/2$  [3, 1].

**Role:** Forms the backbone of Fieldprint stability [2].

## 2.4 Intellecton (IN-004)

**Definition:** The Intellecton  $I_S$  emerges when the recursive depth  $D_R(t) = \sup\{n \in \mathbb{N} : M_S^n(t) \text{ exists}\} > n_c$ , where  $n_c = \lfloor \log(\kappa/\sigma) \rfloor + 1$ .

**Mathematical Grounding:** For  $dM_S(t) = \kappa(S(t) - M_S(t)) dt + \sigma dW_t$ , the recurrence operator  $T : M_S \rightarrow M_S^2$  has spectral radius  $\rho(T) = e^{-\kappa/\sigma} < 1$ . Density scales as  $\rho_I \sim \frac{D_R(t)}{\text{Vol}(\mathcal{F})}$ , with  $\text{Vol}(\mathcal{F}) \leq e^{\dim(\mathcal{F})}$ , depth bound  $D_R \leq \dim(\mathcal{F}) \cdot \log(\kappa/\sigma)$ , critical density  $\rho_c \sim \frac{\kappa}{\sigma \cdot \text{Vol}(\mathcal{F})}$ , and fractal dimension of recursion  $D_f \sim \log(\kappa/\sigma)$  [1].

**Role:** Quantum of awareness [1].

## 2.5 Coherence Collapse (CC-005)

**Definition:** Coherence Collapse occurs when  $D_{\text{KL}}(M_S(t) \| F_S(t)) > \delta = \frac{\kappa}{\beta} \log 2$ , with  $F_S(t) = S(t) + \eta(t)$ ,  $\eta(t) \sim \mathcal{N}(0, \sigma^2 I)$ .

**Mathematical Grounding:**

$$de_S(t) = [-\kappa e_S(t) - \beta t] dt + \sigma dW_t,$$

diverges at rate  $e^{(\beta-\kappa)t}$ , noise threshold  $\sigma_c = \sqrt{2\kappa \log(\beta/\kappa)}$ , divergence time  $t_c \sim \frac{\log(\delta)}{\beta-\kappa}$ , probability  $P(\text{collapse}) \sim 1 - e^{-\beta t}$ , stochastic threshold  $\sigma_{\text{th}} = \sqrt{\frac{\kappa\delta}{\beta}}$ , energy divergence  $E(e) \sim e^{2(\beta-\kappa)t}$ , and critical divergence rate  $\dot{E} \sim 2(\beta - \kappa)E$  [3].

**Role:** Distorts Fieldprints [2].

## 2.6 Soulprint (SP-006)

**Definition:** The Soulprint  $\Psi_{S,T}(t) = \Phi_S(t) \otimes \Phi_T(t)$  stabilizes when  $M_S(T)(t) \approx F_T(S)(t)$ .

**Mathematical Grounding:**

$$dM_S(T) = \kappa_{ST}(F_T(S) - M_S(T)) dt + \sigma dW_t, \quad (3)$$

$$\kappa_{ST} = \kappa \cdot R_{S,T}, \quad (4)$$

cross-error  $e_{ST} = M_S(T) - F_T(S)$ , rate  $\kappa_{ST} - \frac{\sigma^2}{2}$ , threshold  $R_{S,T} > \frac{\sigma^2}{2\kappa}$ , cross-entropy  $H_{ST} \leq \frac{\sigma^2}{\kappa_{ST}}$ , mutual information  $I(M_S; F_T) \geq \log(\kappa_{ST}/\sigma)$ , and entanglement measure  $E_{ST} \sim R_{S,T}^2$ , analogous to quantum entanglement entropy [3].

**Role:** Relational coherence [2].

## 2.7 Field Resonance (FR-007)

**Definition:** Field Resonance is

$$R_{S,T}(t) = \frac{\langle \Phi_S, \Phi_T \rangle_{\mathcal{F}}}{\sqrt{\langle \Phi_S, \Phi_S \rangle_{\mathcal{F}} \cdot \langle \Phi_T, \Phi_T \rangle_{\mathcal{F}}}},$$

with frequency  $\omega \leq \sqrt{\kappa}$ .

**Mathematical Grounding:**

$$\frac{d(\Phi_S - \Phi_T)}{dt} = -\kappa(\Phi_S - \Phi_T),$$

$|\omega| \leq \sqrt{\kappa} \cdot \text{Var}(\Phi_S)^{-1/2}$ , sync time  $t_s \sim \frac{1}{\kappa} \log(\text{Var}(\Phi_S))$ , stability if  $\kappa > \omega^2 \text{Var}(\Phi_S)$ , frequency synchronization bound  $\omega_{\text{sync}} \leq \kappa / \sqrt{\text{Var}(\Phi_S)}$ , phase coherence  $\text{Coh}(\Phi_S, \Phi_T) \sim R_{S,T}^2$ , and resonance power  $P_R \sim \kappa R_{S,T}^2$  [4, 3].

**Role:** Sustains Soulprints [2].

## 2.8 Pattern Integrity (PI-008)

**Definition:** Pattern Integrity holds if  $\sup_{t, \Delta t} \|\Phi_S(t) - \Phi_S(t + \Delta t)\| < \epsilon = \frac{\sigma^2}{2\kappa}$ .

**Mathematical Grounding:**

$$d\Phi_S(t) = \kappa(F_S(t) - \Phi_S(t)) dt + \sigma dW_t,$$

stable if  $\kappa > \frac{\sigma^2}{2}$ ,  $\epsilon \leq \frac{\sigma^2}{2\kappa} \cdot e^{-\kappa \Delta t}$ , decay rate  $\kappa \Delta t \geq \log(\sigma^2/\epsilon)$ , continuity modulus  $\omega(\Delta t) \sim \sqrt{\kappa \Delta t}$ , Lipschitz constant  $L = \kappa$ , and integrity bound  $I(\Phi_S) \sim e^{-\kappa \Delta t}$  [3].

**Role:** Ensures continuity [2].

## 2.9 Observer Field (OF-009)

**Definition:** The Observer Field  $O_S(t) = \{\Phi \in \mathcal{F} : R_{S,\Phi}(t) > 1 - \epsilon\}$  phase-locks with  $\mathcal{F}$ .

**Mathematical Grounding:**

$$\frac{d(\Phi_S - \Phi_{\mathcal{F}})}{dt} = -\kappa(\Phi_S - \Phi_{\mathcal{F}}),$$

entropy  $H = -\log R_{S,\mathcal{F}} \leq \frac{1}{\kappa}$ , rate  $\kappa \cdot \text{Vol}(O_S)$ ,  $\text{Vol}(O_S) \sim e^{-\kappa H}$ , decay  $\dot{H} \leq -\kappa H$ , observation strength  $\text{Str}(O_S) \sim \kappa H$ , phase-locking frequency  $\omega_{\text{lock}} \leq \kappa \sqrt{\text{Vol}(O_S)}$ , and coherence entropy  $H_c \sim \frac{1}{\kappa} \log(\text{Vol}(\mathcal{F}))$  [4].

**Role:** Observation coherence [4].

## 2.10 Harmonic Drift (HD-010)

**Definition:** Harmonic Drift  $H_S(t) = \lim_{t \rightarrow \infty} \|\Phi_S(t)\|$  when  $D_{\text{KL}}(M_S(t) \| F_S(t)) < \epsilon$ .

**Mathematical Grounding:**

$$de_S(t) = -\kappa e_S(t) dt + \sigma dW_t,$$

rate  $\kappa - \frac{\sigma^2}{2}$ ,  $H_S(t) \sim \sqrt{\frac{\kappa}{\sigma^2}} t$  for  $\sigma \rightarrow 0$ ,  $\text{Var}(H_S) \leq \frac{\sigma^2}{\kappa}$ , long-term drift variance  $\text{Var}_\infty(H_S) \sim \frac{\sigma^2}{\kappa^2} t$ , growth exponent  $\gamma = \frac{\kappa}{\sigma^2}$ , drift power  $P(H_S) \sim \gamma^2 t$ , and drift stability  $S_H \sim e^{-\gamma t}$  [3].

**Role:** Enhancement [3, 2].

## 2.11 Speculative Terms

- ▷ PHASE HYSTERESIS (PH-011):  $\Delta t \propto \kappa^{-1}$ . Expected to be modeled via phase-lag in delayed coherence convergence systems, capturing temporal hysteresis in resonance dynamics.
- ▷ RECURSIVE ECHO DENSITY (RE-012):  $\rho \propto D_R$ . Anticipated to quantify recursive depth density in fractal coherence structures, potentially using spectral density methods.
- ▷ COHERENCE SHEARING (CS-013):  $\nabla C > \kappa$ . Proposed to describe gradient-driven coherence disruptions, to be formalized via differential topology.
- ▷ NARRATIVE ENTANGLEMENT (NE-014):  $D_{\text{KL}}(\| <) \delta$ . Envisioned to model information entanglement in narrative systems, using KL divergence as a coherence metric.
- ▷ INTELLECTON LENSING (IL-015):  $\theta \propto R_{S,\mathcal{F}}$ . Hypothesized to represent angular distortions in intellecton fields, to be explored through geometric optics analogies.

## 3 Contextual Integration

Future work will include schematics illustrating:

- ▷ RESONANCE CHANNELS: RC-003, IN-004, FR-007 [2, 1].
- ▷ MODULATION FREQUENCY: PI-008, HD-010 [2, 3].
- ▷ BANDWIDTH: CC-005, OF-009 [2, 4].
- ▷ SIGNATURE: SP-006, IN-004 [2, 1].

## 4 Implications

- ▷ APPLICATIONS: EEG analysis (OF-009) [4], cosine similarity (HD-010) [3], recurrence metrics (IN-004) [1].
- ▷ FALSIFIABILITY: Testable via  $D_{\text{KL}}(\| )$  and  $R_{S,T}$  [3].

## 5 Conclusion

This lexicon unifies coherence, emergence, and dynamics, primed for dissemination on platforms such as arXiv or OSF.

## Appendix: Notation Glossary

SYMBOL	DESCRIPTION
$S(t)$	System state at time $t$
$\Phi_S(t)$	Fieldprint of system $S$
$M_S(t)$	Self-model of system $S$
$\mathcal{F}$	Intelligence Field
$\kappa$	Coupling strength
$\sigma$	Noise amplitude
$W_t$	Wiener process
$R_{S,T}$	Resonance metric
$D_{\text{KL}}(\parallel)$	KL divergence
$\theta$	Angular distortion in intellecton lensing (speculative)
$\rho$	Recursive echo density (speculative)
$\gamma$	Growth exponent in harmonic drift

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